

Lesson 1, Polynomials, E050

POLYNOMIALS

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Notes:

$$x^m \cdot x^n = x^{m+n}$$

$$\frac{x^m}{x^n} = x^{m-n}$$

$$5x + 3 \Rightarrow \text{Degree 1}$$

$$4x^3 \Rightarrow \text{Degree 3}$$

Notes: see

1. power index + graphs, pdf

②. watch Youtube
SUN P0001

Exercise 1: (1)

$$(2x^3 - 4x + 1) \times (3x^3 - x^2 - 2)$$

Solve 1:

$$6x^6 - 2x^5 - 4x^3$$

$$(2x^3 - 4x + 1) \times (3x^3 - x^2 - 2)$$

Solve 2 :

$$-12x^4 + 4x^3 + 8x$$

$$(2x^3 - 4x + 1) \times (3x^3 - x^2 - 2)$$

Solve 3:

$$3x^3 - x^2 - 2$$

Then, add for multiplying,

$$= 6x^6 - 2x^5 - \cancel{4x^3} - 12x^4 + \cancel{4x^3} + 8x + \underline{3x^3 - x^2 - 2}$$

$$= 6x^6 - 2x^5 - 12x^4 + 3x^3 - x^2 + 8x - 2$$

##

Exercice 2. Expand

$$(2x-3)(x^2-4x+2)$$

Find the coefficient of x^3 in expansion.

Solution:

1st:

$$(2x-3)(x^2-4x+2)$$

$$\text{solve 1: } 2x^3 - 8x^2 + 4x$$

2nd:

$$(2x-3)(x^2-4x+2)$$

$$\text{solve 2: } -3x^2 + 12x - 6$$

$$\text{add by multiplying: solve 1 + solve 2} = 2x^3 - 8x^2 + 4x - 3x^2 + 12x - 6$$

Therefore, coefficient

$$= 2x^3 - 11x^2 + 16x - 6$$

$$= 2x^3 - 11x^2 + 16x - 6$$

#

Problems. Find the sum and difference of polynomials.

$$C1) (a + 2b + 4c) + (2a + b + 3c)$$

$$C2) (5x - 3y + 2z) + (4x + y - 3z)$$

$$C3) (a^2 - b^2 - c^2) + (2a^2 - 3b^2 + 4c)$$

$$C4) (-10r^2 + 7s^2 - 5t^2) - (9r^2 - 6s^2 + 3t^2)$$

$$C5) (12f^2 + 21fg - 18g^2) - (-5f^2 + 8g^2 - 1)$$

$$C6) (1 - c^2 + c^4) - (-5c^3 - 3c^2 + c^4)$$

$$C7) (10a - 5b^2 + 6) + (-3b + 7b^2 - 3)$$

$$C8) (5x^2 + 4xy - 3) - (6x^2 + 12xy - 4y^2 + 5)$$

$$C9) - (5p + 3) + (6p + 3) - 3p + (p - 1)$$

$$C10) (12x + y + z) + (2x - 5y) - (5x - y + z)$$

$$C11) (-a - b + c) - (a - c - b) - (a + c - b)$$

$$C12) (3x + 2y - 5z) - (7x + 4z) + (2x + y + 5z)$$

$$C13) (x^4 + 3x^3 - x^2 - x - 1) - (x^3 + x^2 - x + 1)$$

$$C14) (a - 2b - c) - 2b - (3a - 3c) + c - (b - a)$$

After seeing

①. power index + graphs
+ pdf

②. Then, calculate

from page ③.

to page ④.

Find the product of polynomials and monomials.

c a) $5(a+b+c)$

c b) $-2(cx+2y-3z)$

c c) $12(u^2-uv^3)$

c d) $4(12a^2b-9ab-15ab^2)$

c e) $2x(ab-bc+ac)$

c f) $x(x^3+2+xy)$

c g) $2x^2y^6z^5 \times 8x^3y^7z^2$

c h) $(x+y)(a+b)$

c i) $c(2a+b)(3a^2+4a-b)$

c j) $(3b+5c-2d)(4c+3d)$

Simplify the polynomials

$$(1) [(7-a) \times 3 - 5 \times (2-a)] \times 4$$

$$(2) 5[7(x-2y) - 6(2x-y)]$$

$$(3) 1 - [2(3a-2b) + 3(2a-3b)]$$

$$(4) -2x - [-3x - (-4x)] - [x - (-3x)]$$

$$(5) 5s - 3[(2s-1) \times 8s - 7]$$

$$(6) -8a - [-8a - [-8a - (-8a)]]$$

$$(7) (x^2 + y^2)x - xy(2y)$$

$$(8) (0.2a - 0.5b)7a - (0.4a + 0.6b)3b$$

$$(9) 2(2x-3y) - [6(x-4y) - (2x-y)]$$

$$(10) 2(x-1)(2x+2)^3 [4(x-1) + (2x+2)]$$

Find the quotient of polynomials.

C : = divided by)

↓

call 'is to'

c1) $25a^2 : 5a$

c2) $10xy^2 : 5xy$

c3) $20x^2y^6z^2 : 4x^2y^5z$

c4) $(2x^2 - 4x) : 2x$

c5) $(12 + 6z) : 6$

c6) $(4ab - b^2) : b$

c7) $(2a^2b^4 - 7a^2b^3) : a^2b^2$

c8) $(xy^4 - x^4y^3 + y^2) : y^2$

c9) $(-4s^3 + s^2) : (-s)$

c10) $(-18p + 12q + 6r) : (-6)$

Problems:

Find the quotient of two polynomials.

C : = divided by)
↓
call 'is to'

C1) $(2x^3 + 3x^2 + x + 6) : (x+2)$

C2) $(x^3 - 2x^2 + 1) : (x-1)$

C3) $(2x^4 + 3x^3 - 3x^2 + 3x - 5) : (2x+5)$

C4) $(-x^4 + x^3 - 4x^2 + 7x - 3) : (-x+1)$

C5) $(2x^3 - 3x^2 - 10x + 3) : (x-3)$

C6) $(x^3 + 2x^2 - 13x + 10) : (x+5)$

C7) $(x^4 + x^3 - x - 1) : (x^2 - 1)$

C8) $(9x^3 + 18x^2 - 18x - 9) : (3x-3)$

C9) $(2x^3 - x^2 + x + 2) : (2x+1)$

C10) $(6x^3 - 7x^2 + 5) : (2x-1)$